

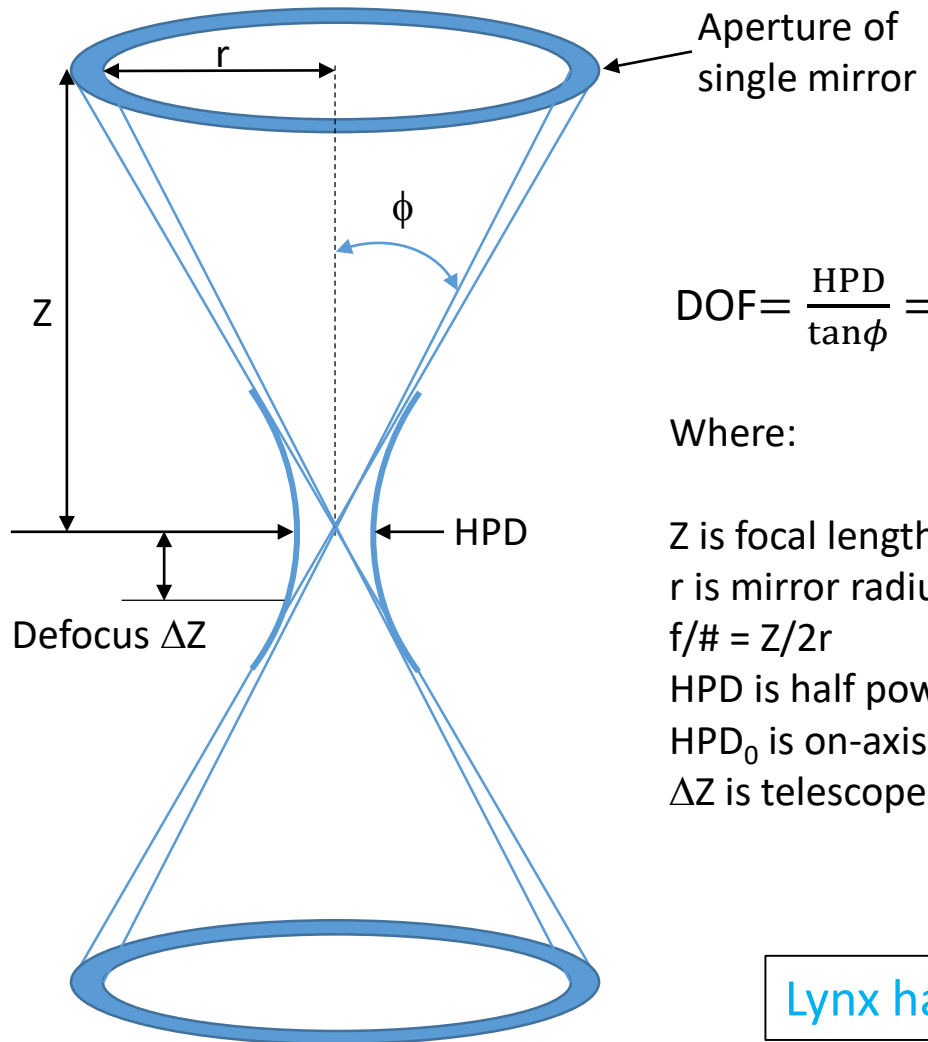
Lynx Telescope Mirror Physics

Part 2: Depth of Focus and Field of View (DOF and FOV)

Lynx Optics Working Group
August 30, 2017



Telescope Mirror Depth of Focus (DOF)



$$\text{DOF} = \frac{\text{HPD}}{\tan \phi} = 2 * \text{HPD} * f/\#$$

Where:

Z is focal length

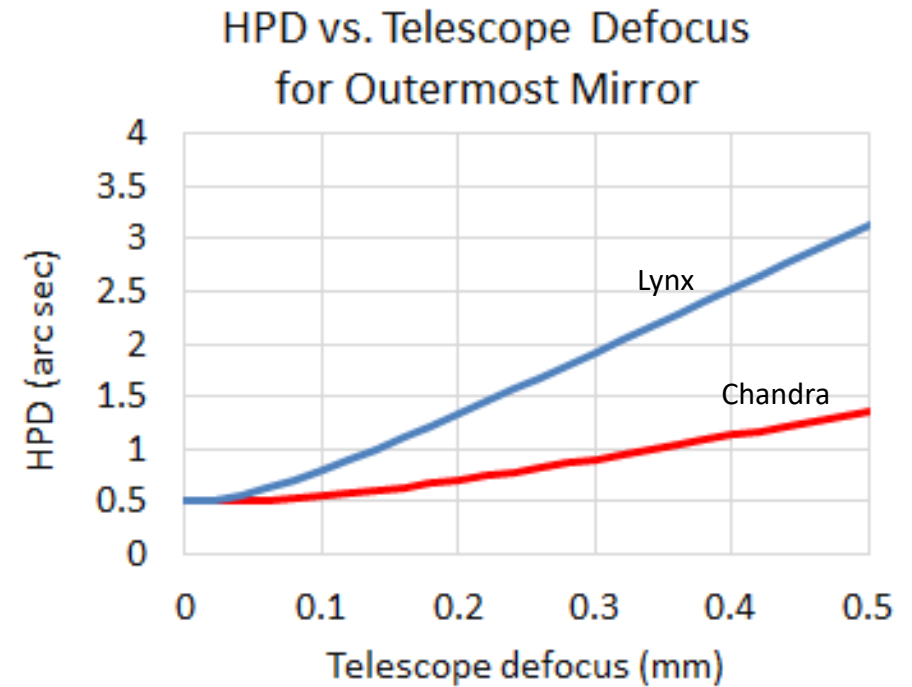
r is mirror radius

$f/\# = Z/2r$

HPD is half power diameter

HPD_0 is on-axis HPD

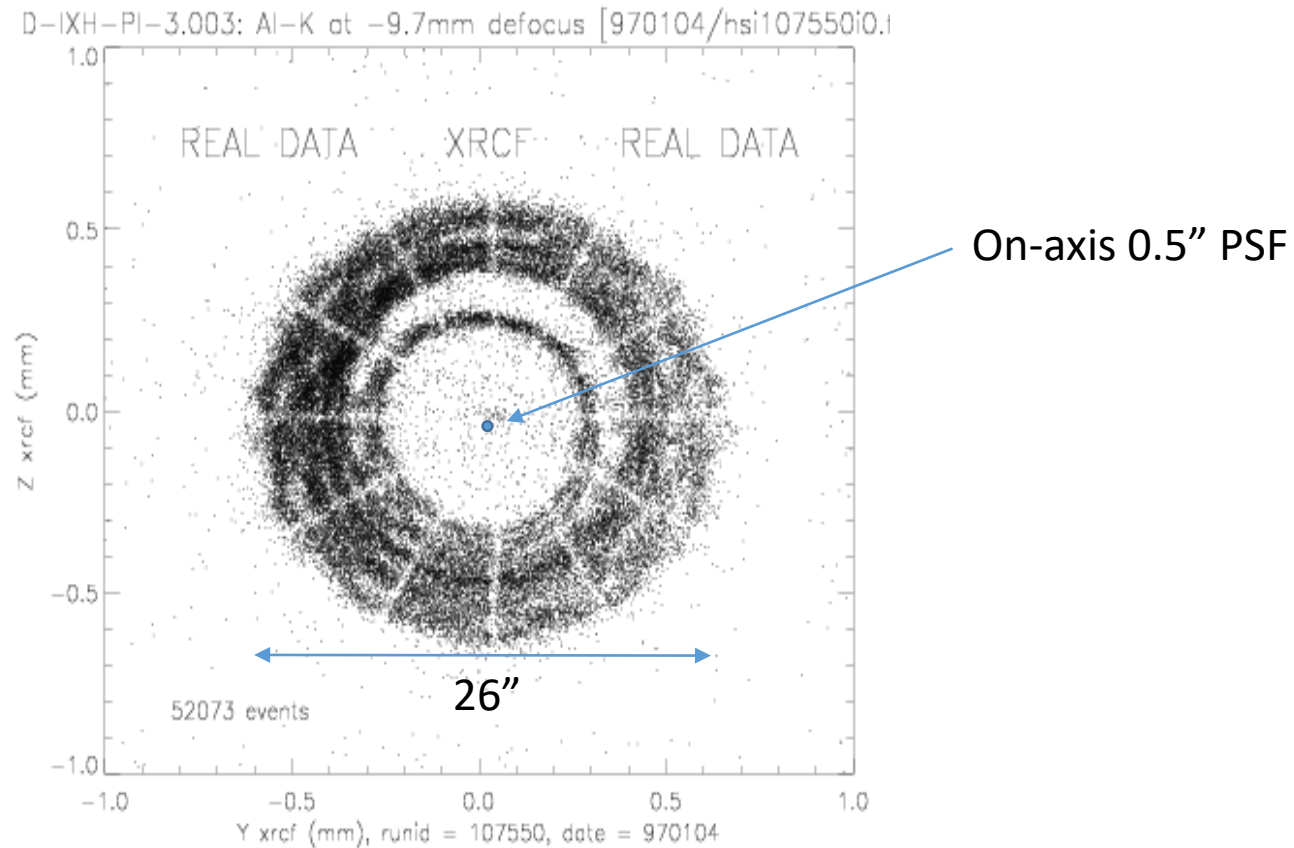
ΔZ is telescope defocus



$$\text{HPD}(\Delta Z) = \sqrt{\text{HPD}_0^2 + \left(\frac{\Delta Z}{f/\#}\right)^2}$$

Lynx has 2.4X tighter focus budget than Chandra

Measured Chandra Telescope PSF De-Focused by 9.7 mm



<http://space.mit.edu/CXC/MARX/indetail/hardwaremodel.html>

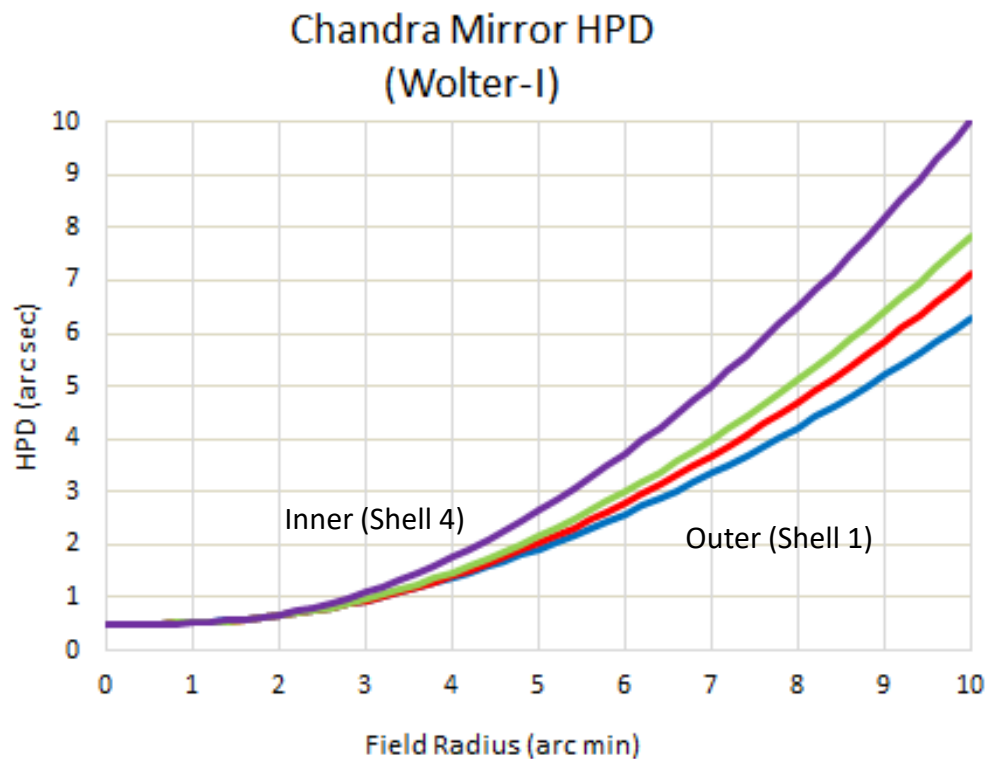
Parametric Studies of Chandra vs. Lynx

| Mission | Chandra | Lynx |
|------------------------------|---------|------|
| Focal Length, F (m) | 10 | 10 |
| Min diameter, D_{\min} (m) | 0.65 | 1 |
| Max diameter, D_{\max} (m) | 1.23 | 3 |
| Length, L (m) | 0.84 | 0.2 |



Warning!
Simulations do not take into account vignetting.
Ray trace follow-up required!

Chandra Field of View (FOV)



Shell 1 Shell 4



Chandra mirrors

Half power diameter (HPD)

$$HPD = 2 \sqrt{\left(0.27 \frac{\tan^2 \theta}{\tan \alpha} \frac{L}{Z} + \tan \theta \tan^2 \alpha\right)^2 + \left(\frac{\lambda}{2L \tan \alpha}\right)^2 + HPD_0^2}$$

Geometry

Diffraction

Engineering

L = mirror length

Z = focal length

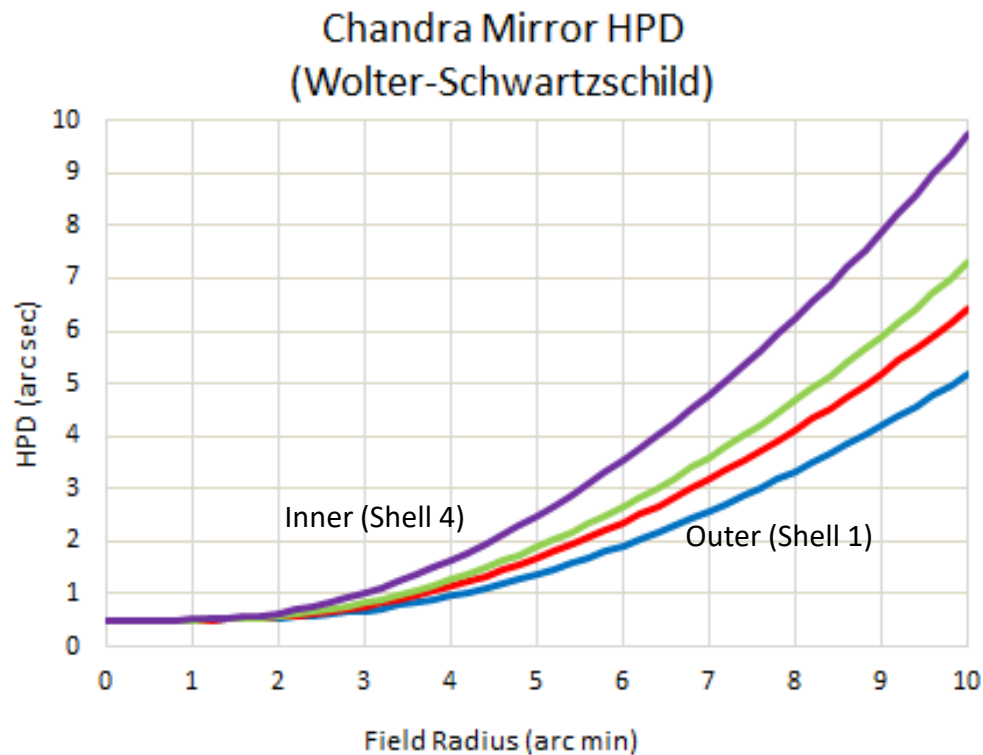
λ = wavelength

α = graze angle

θ = field radius

HPD_0 = on-axis HPD

Chandra Field of View (FOV)



Shell 1 Shell 4



Chandra mirrors

Half power diameter (HPD)

$$HPD = 2 \sqrt{\underbrace{\left(0.27 \frac{\tan^2 \theta L}{\tan \alpha Z}\right)^2}_{\text{Geometry}} + \underbrace{\left(\frac{\lambda}{2L \tan \alpha}\right)^2}_{\text{Diffraction}} + \underbrace{HPD_0^2}_{\text{Engineering}}}$$

L = mirror length

Z = focal length

λ = wavelength

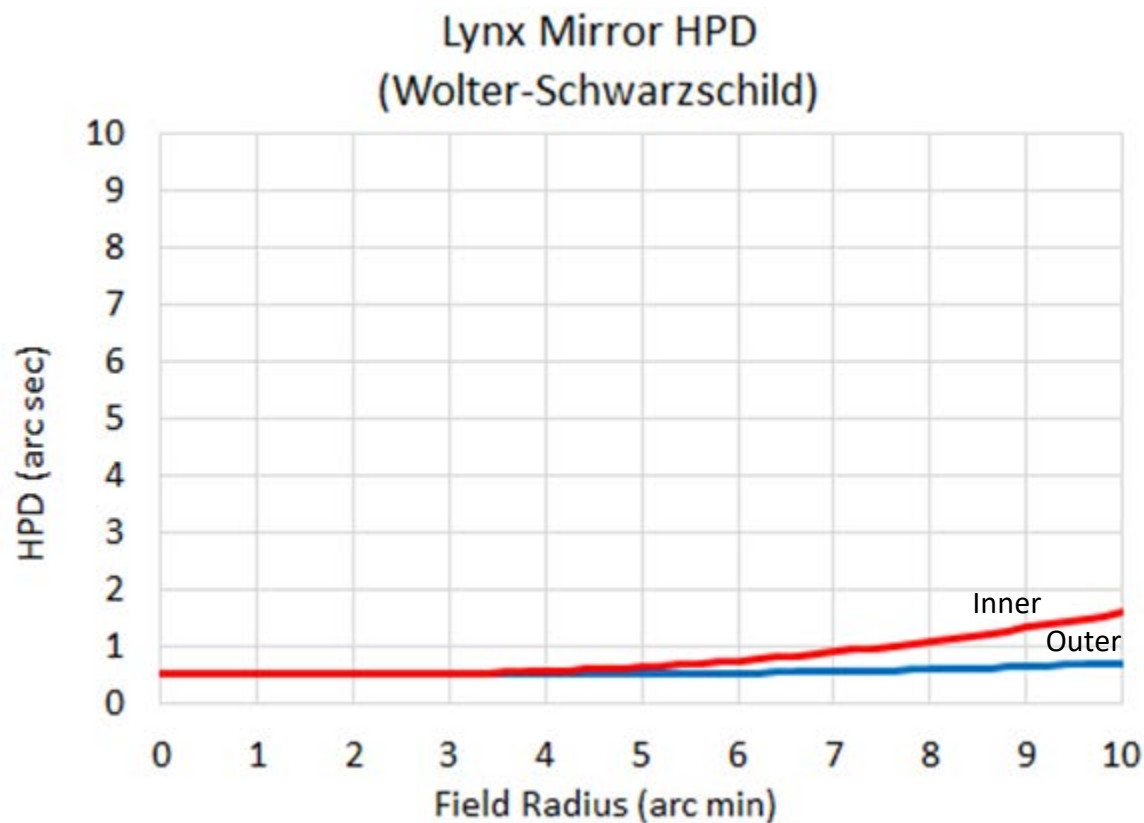
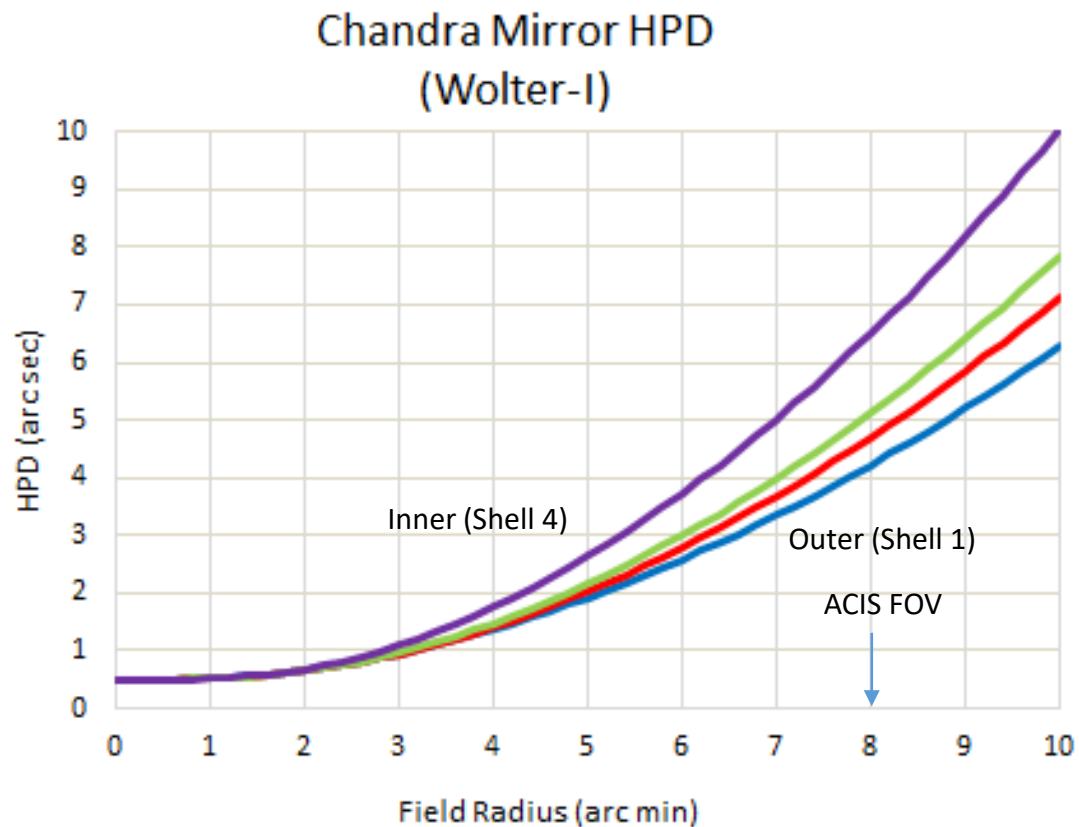
α = graze angle

θ = field radius

HPD_0 = on-axis HPD

Both geometry and
diffraction degrade
HPD of inner mirrors

Chandra vs. Lynx FOV



Lynx has >3X wider FOV compared to Chandra (10X smaller $L/\tan\alpha$)

$$HPD_g = 0.27 \frac{\tan^2 \theta}{\tan \alpha} \frac{L}{Z}$$

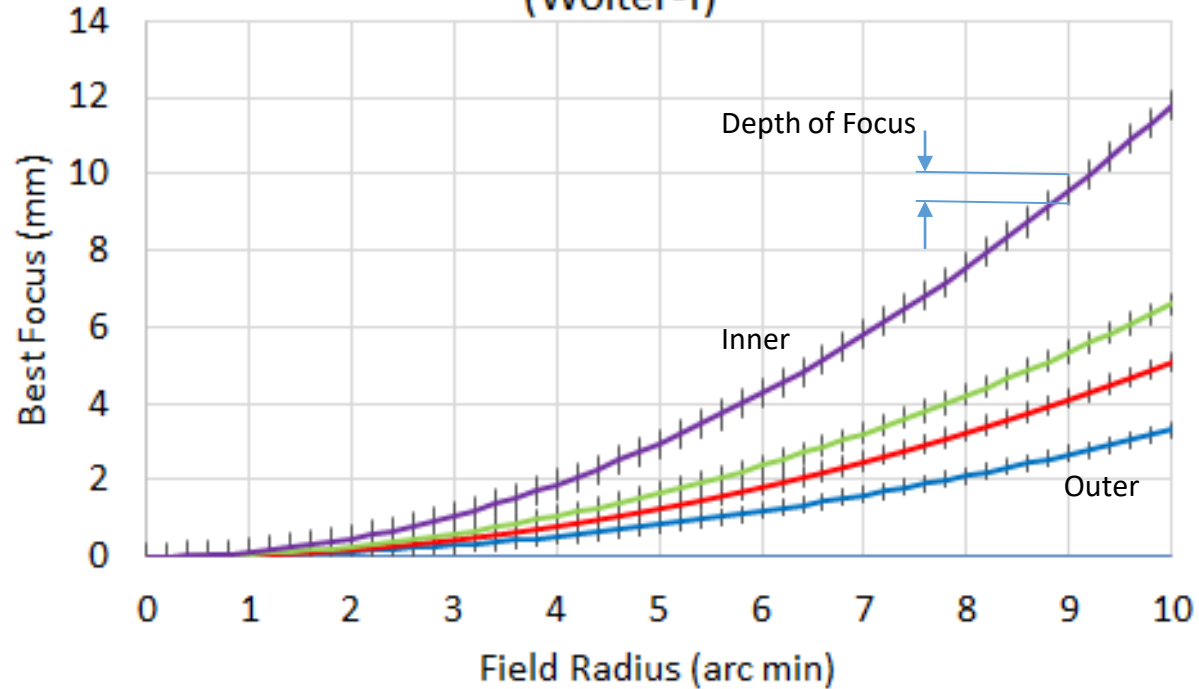
But wait, there's more ...

Lynx focal plane is much flatter than Chandra's!

Chandra Focal “Plane”

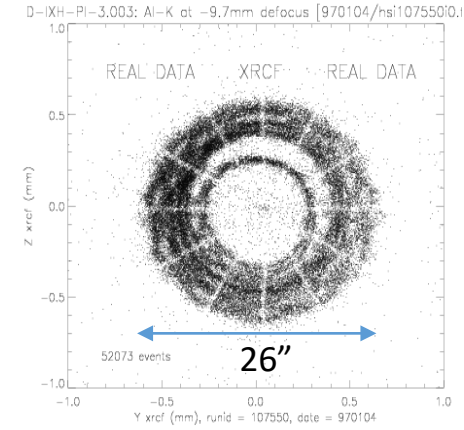
X-ray telescopes do not have a flat focal surface!

Chandra Mirror -- Focal Plane Curvature
(Wolter-I)

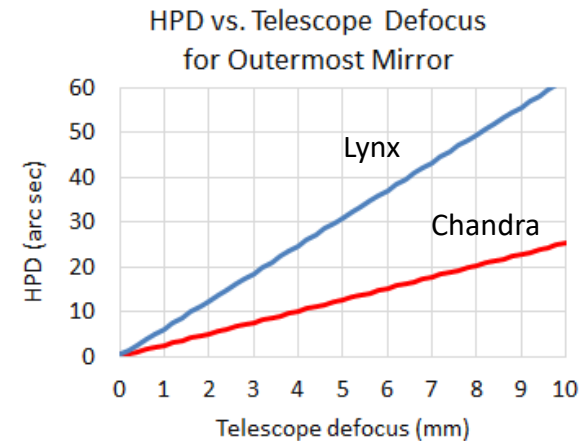


Each shell has a unique
best focal surface

$$\delta = 1.1 L \left(\frac{\tan \theta}{\tan \alpha} \right)^2$$



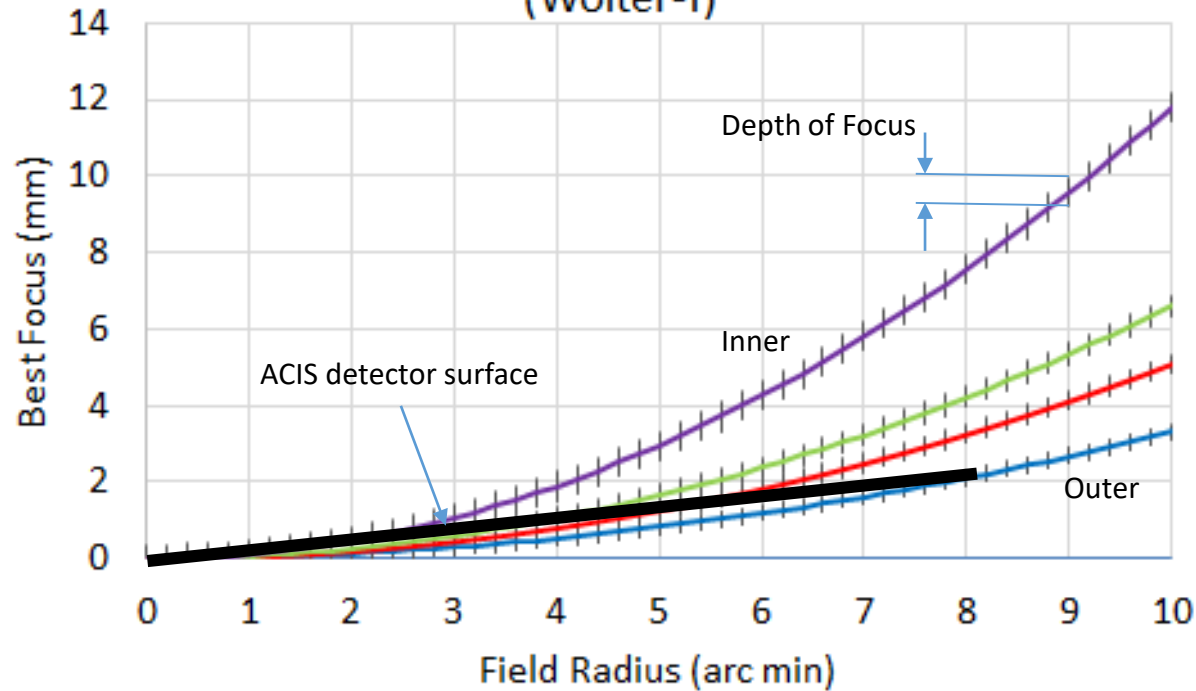
Chandra PSF 9.7 mm defocus



Chandra Focal “Plane”

X-ray telescopes do not have a flat focal surface!

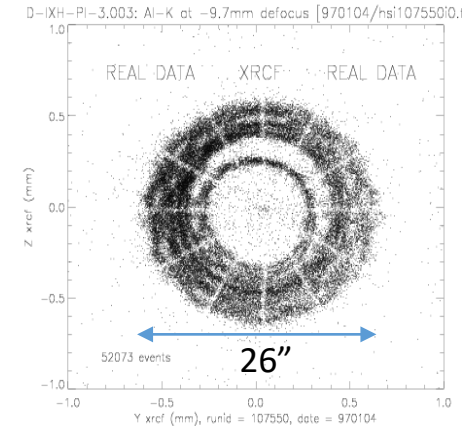
Chandra Mirror -- Focal Plane Curvature
(Wolter-I)



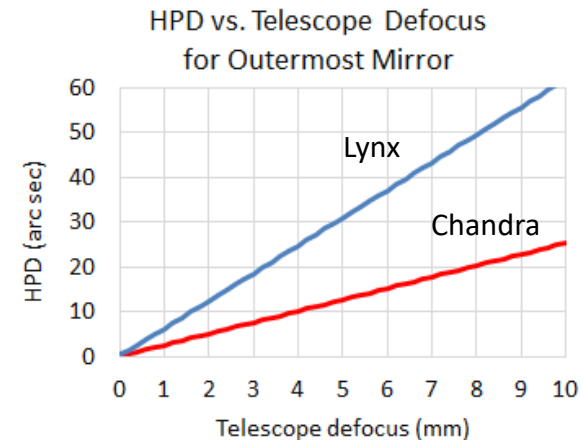
Each shell has a unique
best focal surface

Field sag

$$\delta = 1.1 L \left(\frac{\tan \theta}{\tan \alpha} \right)^2$$

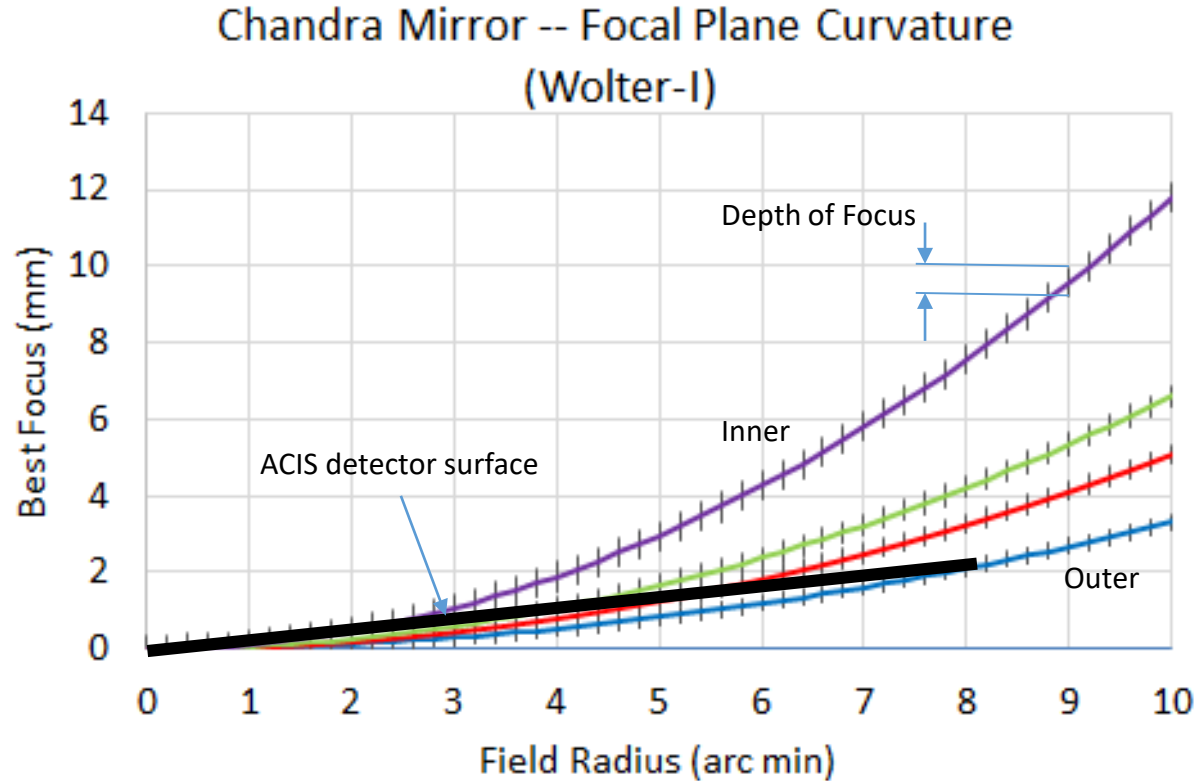


Chandra PSF 9.7 mm defocus



Chandra Focal “Plane”

X-ray telescopes do not have a flat focal surface!



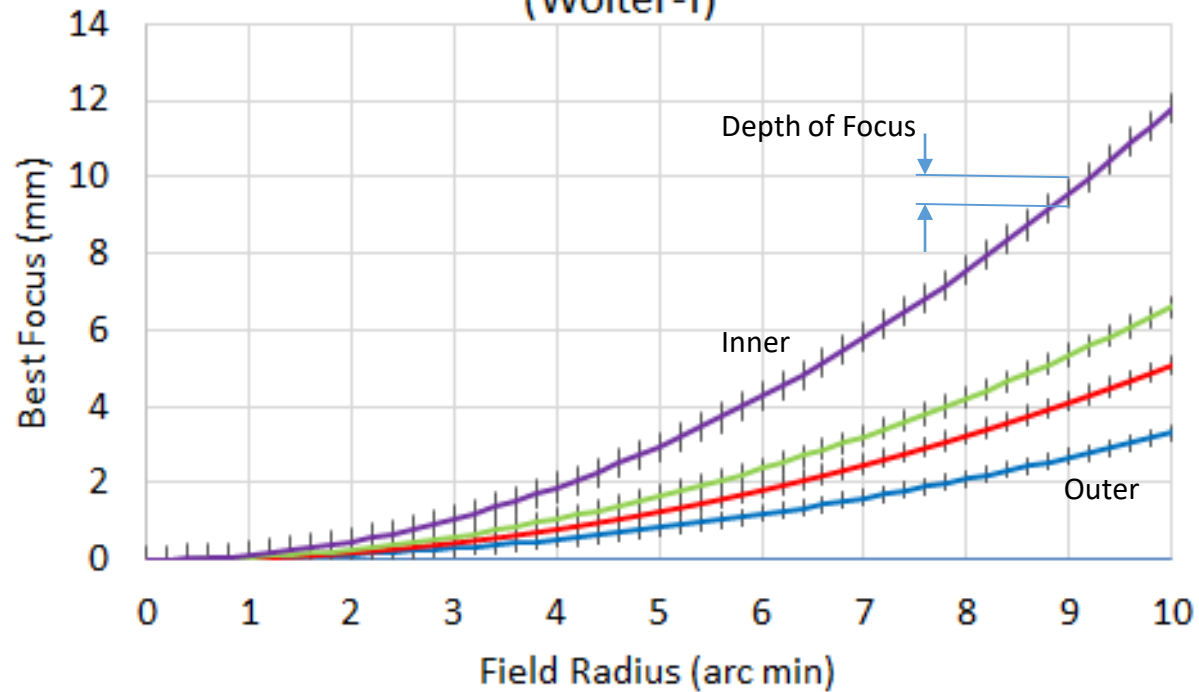
Hard x-rays (inner mirrors) have poor PSF compared to soft x-rays (outer mirrors) for two reasons:

1. PSF is smaller for inner mirrors due to smaller α
2. Detector plane is optimized to outer mirrors!

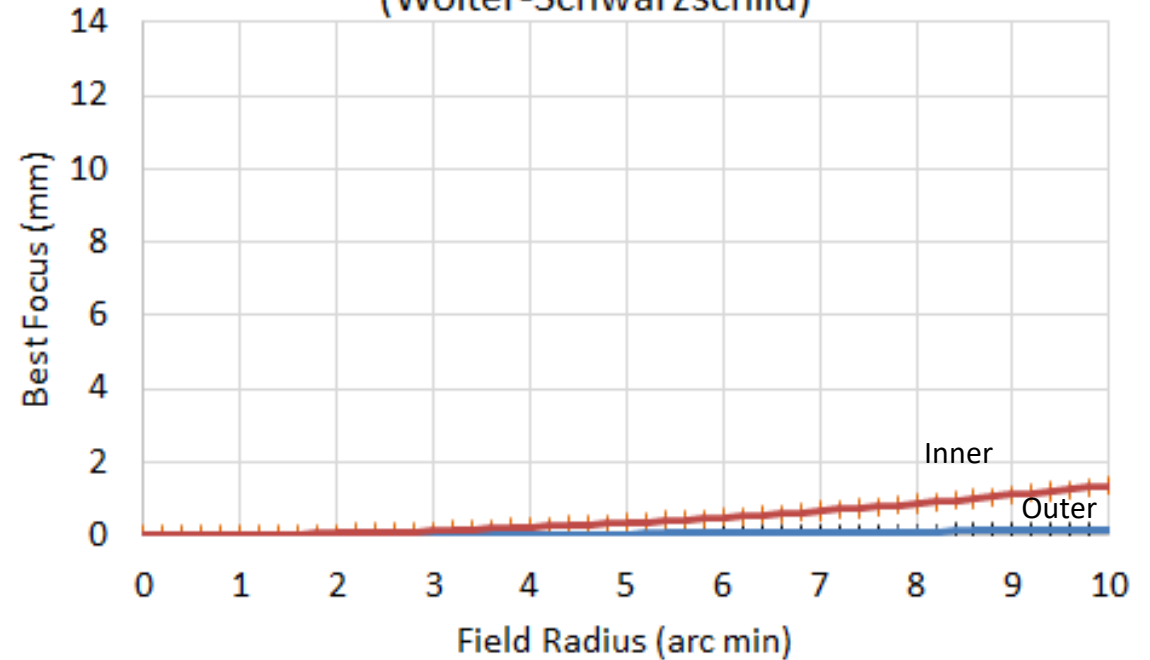
$$HPD_g = 0.27 \frac{\tan^2 \theta}{\tan \alpha} \frac{L}{Z}$$

Chandra vs. Lynx Focal Surfaces

Chandra Mirror -- Focal Plane Curvature
(Wolter-I)



Lynx Mirror -- Focal Plane Curvature
(Wolter-Schwarzschild)

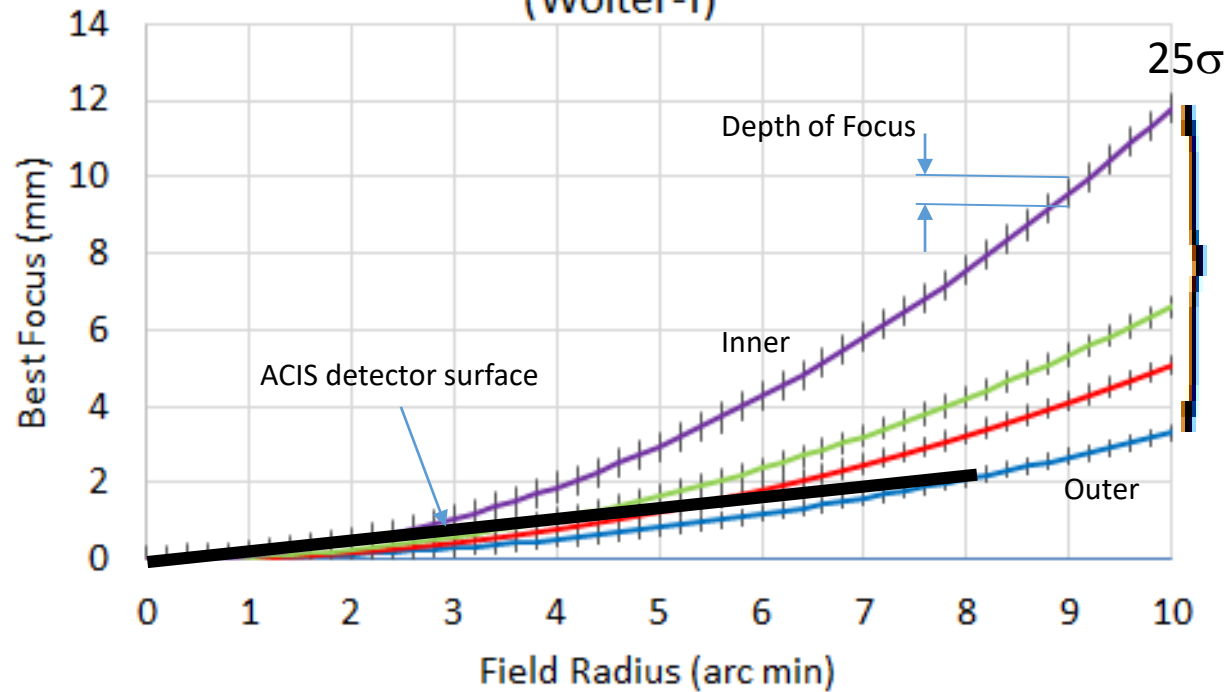


Field sag

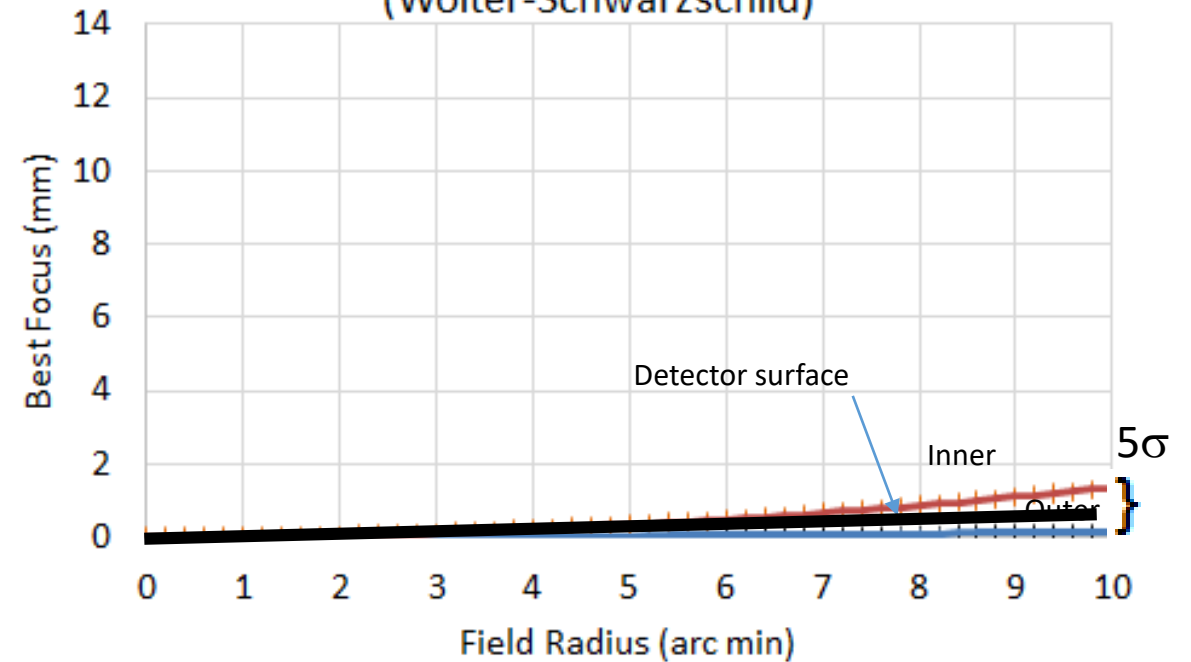
$$\delta = 1.1 L \left(\frac{\tan \theta}{\tan \alpha} \right)^2$$

Chandra vs. Lynx Focal Surfaces

Chandra Mirror -- Focal Plane Curvature
(Wolter-I)

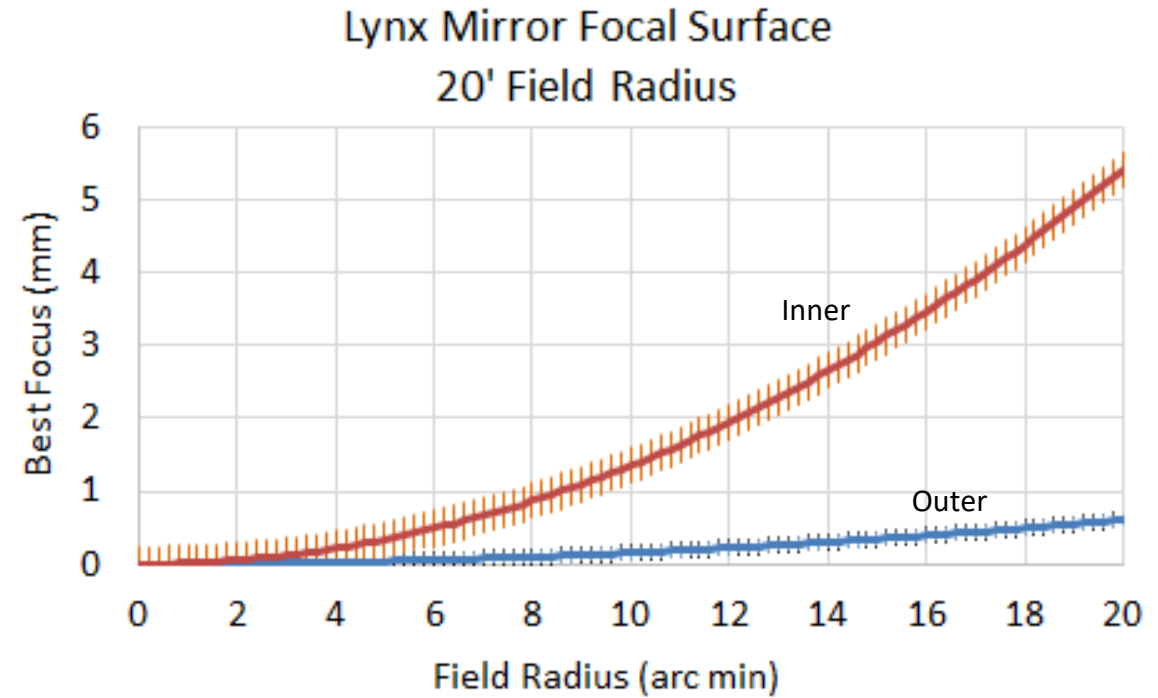
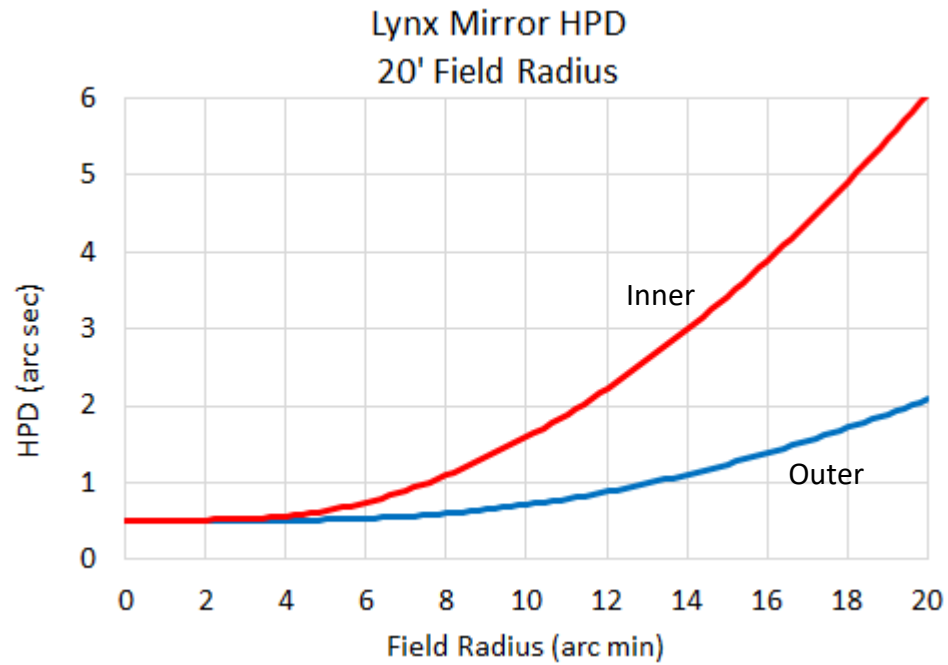


Lynx Mirror -- Focal Plane Curvature
(Wolter-Schwarzschild)

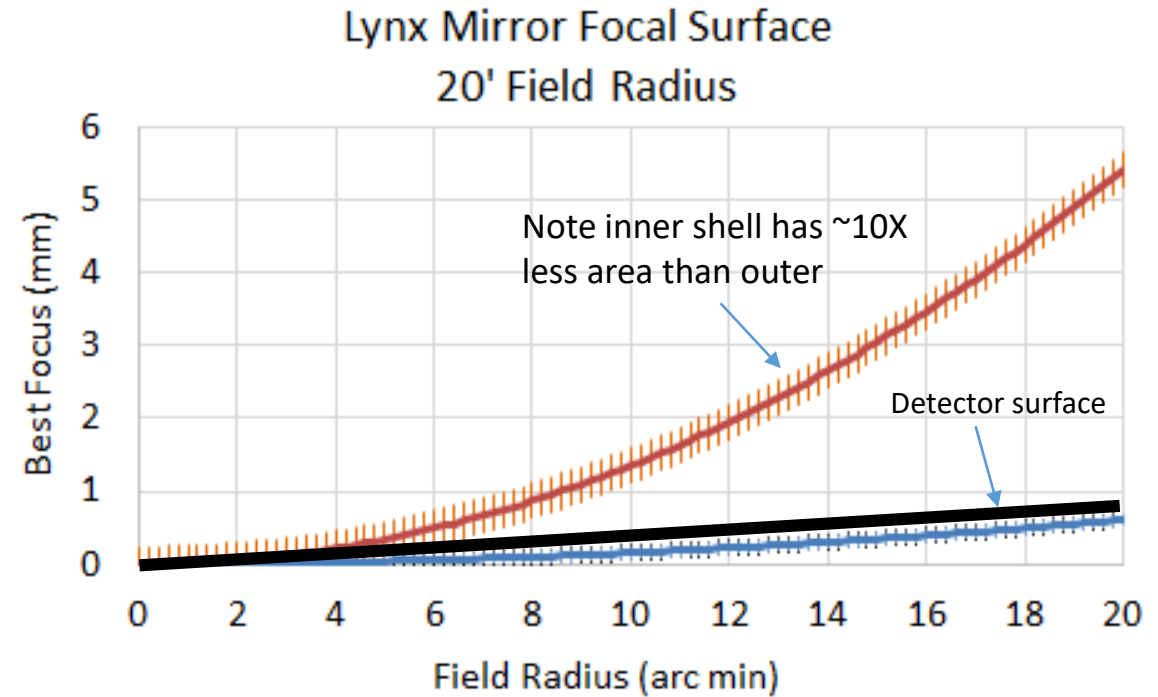
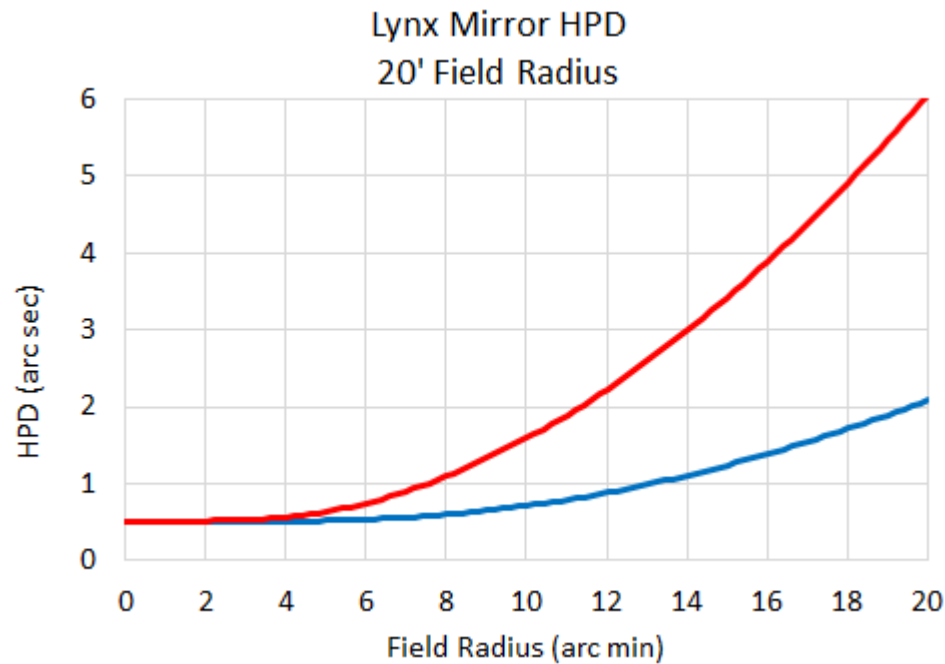


Lynx has ~40X flatter focal surface compared to Chandra!

Lynx with 40' Field of View



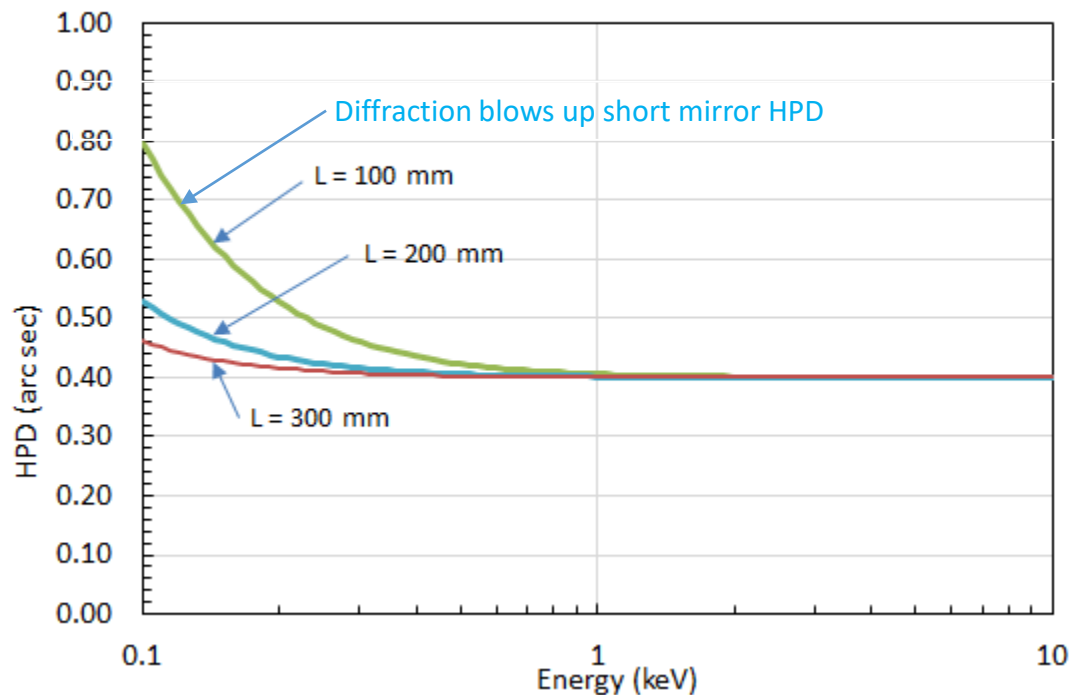
Lynx with 40' Field of View



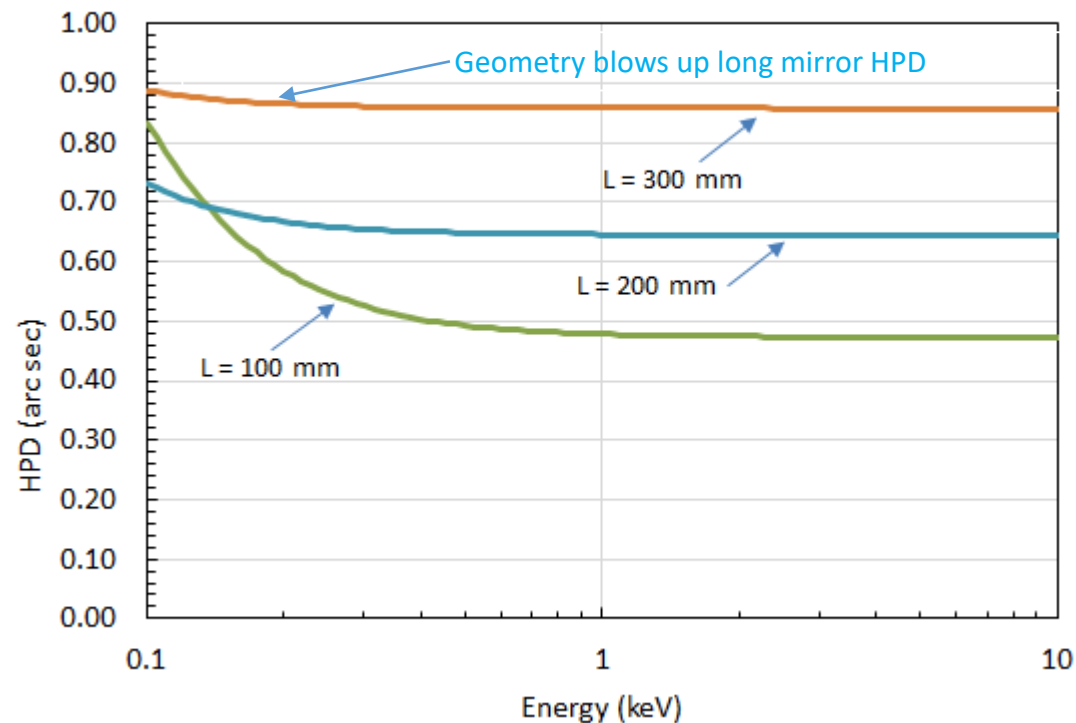
A 40' FOV Lynx "looks like" a 16' FOV Chandra

FOV Tradeoff to Optimize Mirror Length

Lynx On-Axis HPD



Lynx 10' Off-Axis HPD



Half power diameter (HPD)

200 mm-long mirror is sweet spot for Lynx!
(Optimal trade-off of
diffraction and geometry terms)

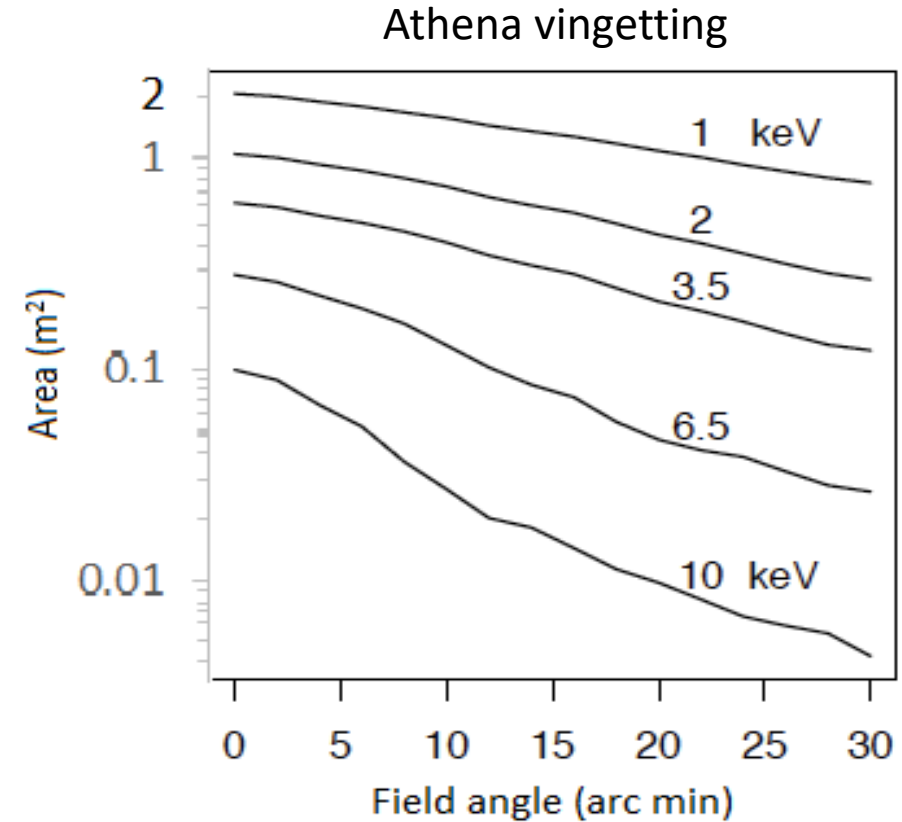
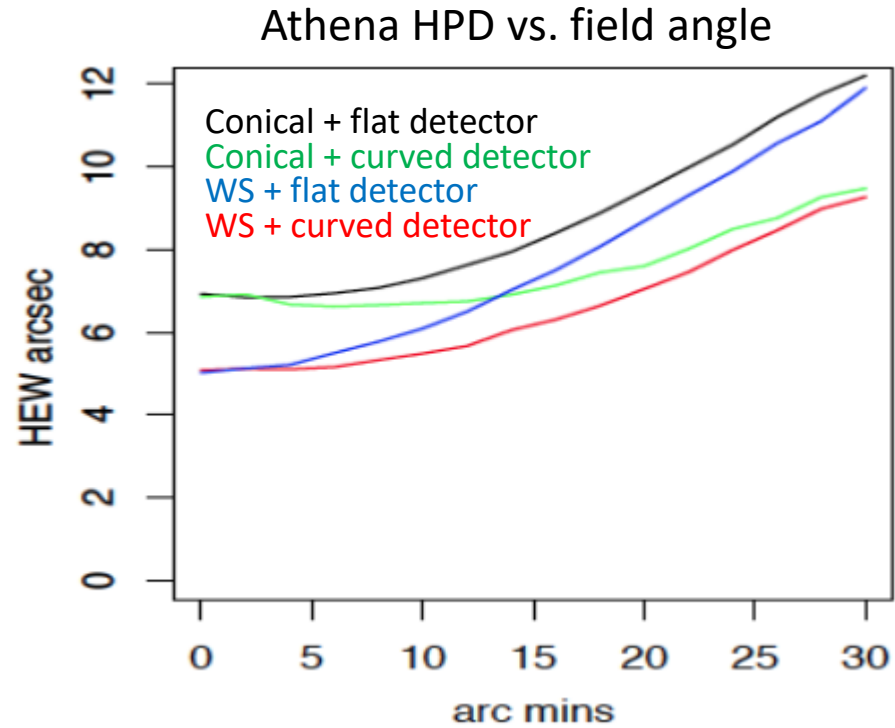
$$HPD = 2 \sqrt{\left(0.27 \frac{\tan^2 \theta}{\tan \alpha} \frac{L}{Z}\right)^2 + \left(\frac{\lambda}{2L \tan \alpha}\right)^2} + HPD_0^2$$

Geometry

Diffraction

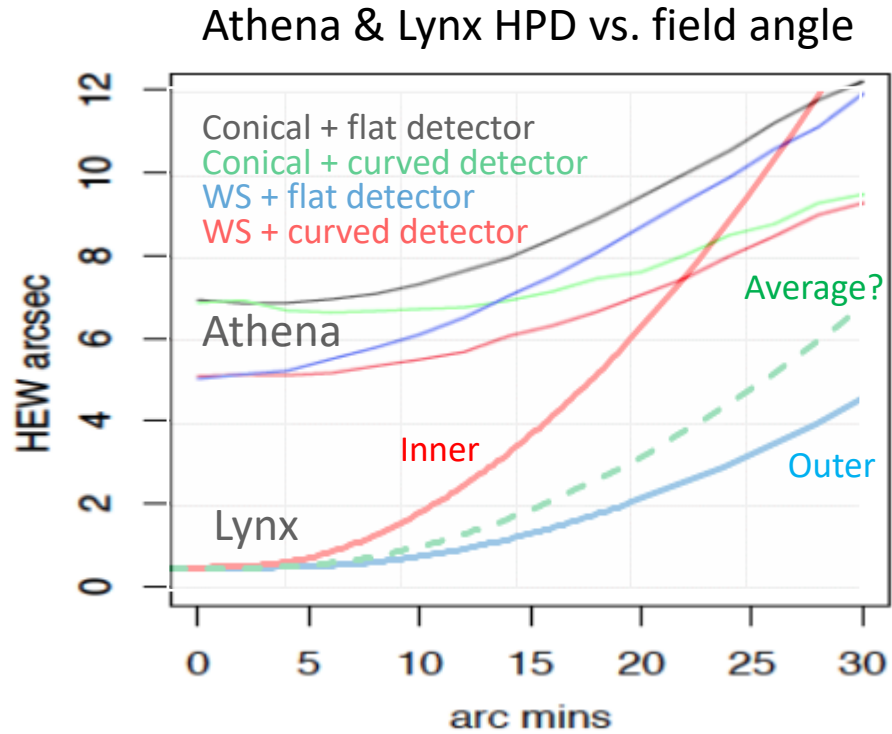
Engineering

Nominal Athena FOV and Vignetting

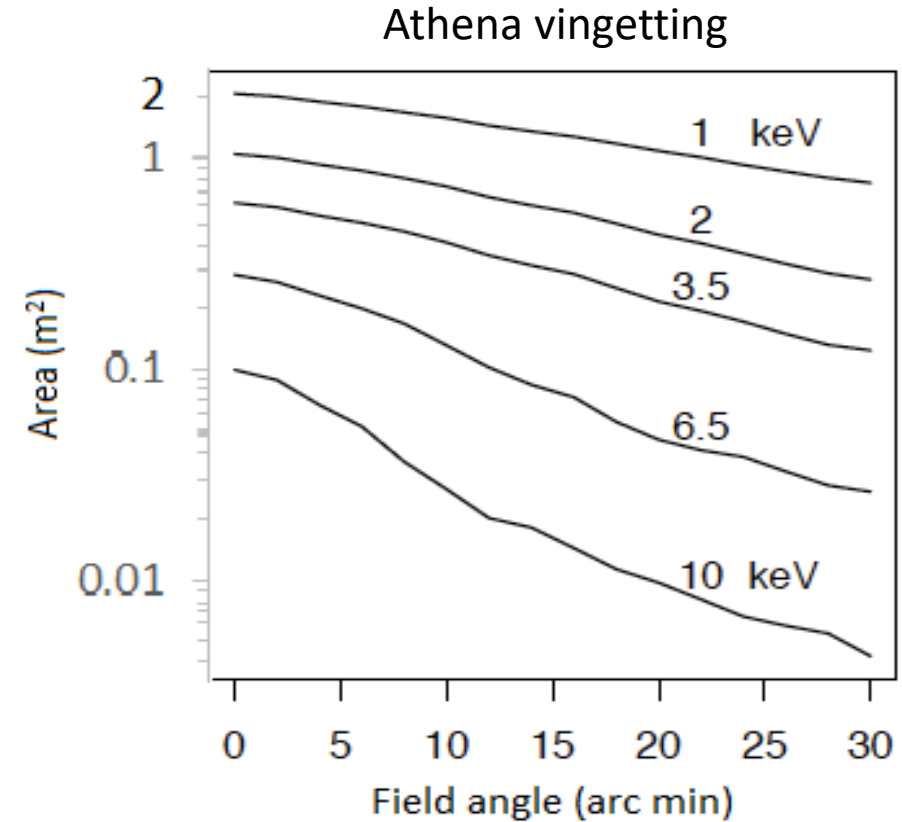


The Hot and Energetic Universe: The Optical Design of the Athena+ Mirror, Willingale et al., 2013.

Lynx vs. Athena FOV



Lynx can challenge Athena in FOV comparison!



Athena @ 1 keV vignettes by 2.5X at 30'

Every proposal tells a story, don't it?

Here is our story:

- Sustained NASA investment has enabled technical advances leading to a $(10X)^4$ more powerful X-ray Surveyor concept ...
- ... in turn enabling exciting, breakthrough science

Why $(10X)^4$?

- 10X larger area
- 10X improved spectral resolution
- 10X better detectors
- 10x larger FOV merit function
(i.e., number of resolvable point sources in FOV)

Large FOV strong selling point for Lynx!

Summary

- Lynx optics performance is huge leap from Chandra:
 - Larger diameter and shorter mirrors have large positive impact on FOV
 - Lynx has a much flatter best-focus surface
 - Geometry and diffraction can be balanced to optimize FOV
- Lynx can challenge Athena in FOV comparison
- Parametric studies need to be backed up with ray traces
 - Vignetting should be considered if $>10'$ FOV ray trace study requested by STDT

Questions?

